

Appendix G

Clausing Factor Monte Carlo Calculation

Visual Basic Monte-Carlo calculation of Clausing Factor for thruster grids.

Inputs:

Clausing Factor Calculator		
Inputs	Radius (mm)	Diameter
thickScreen	0.381	
thickAccel	0.5	
rScreen	0.9525	1.905
rAccel	0.5715	1.143
gridSpace	0.5	
npart	10^6	

Code:

```

Sub Clausing()
    thickScreen = Range("C4")
    thickAccel = Range("C5")
    rScreen = Range("C6")
    rAccel = Range("C7")
    gridSpace = Range("C8")
    npart = Range("C9")
    ' Monte Carlo Routine that calculates Clausing factor for
    CEX
    ' returns Clausing Factor and Downstream Correction
    factor
    Dim gone As Boolean
    Pi = 3.14159265358979
    'assumes rTop = 1

```

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rBottom = rScreen / rAccel
lenBottom = (thickScreen + gridSpace) / rAccel
lenTop = thickAccel / rAccel
Length = lenTop + lenBottom
    iescape = 0
    maxcount = 0
    icount = 0
    nlost = 0
    vztot = 0#
    vz0tot = 0#
For ipart = 1 To npart
    ' launch from bottom
    notgone = True
    r0 = rBottom * Sqr(Rnd)
    z0 = 0#
    costheta = Sqr(1# - Rnd)
    If (costheta > 0.99999) Then costheta =
0.99999
    phi = 2 * Pi * Rnd
    sintheta = Sqr(1# - costheta ^ 2)
    vx = Cos(phi) * sintheta
    vy = Sin(phi) * sintheta
    vz = costheta
    rf = rBottom
    t = (vx * r0 + Sqr((vx ^ 2 + vy ^ 2) * rf
^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)
    z = z0 + vz * t
    vz0tot = vz0tot + vz
    icount = 0
    Do While notgone
        icount = icount + 1
        If (z < lenBottom) Then
            ' hit wall of bottom cylinder and is re-
emitted
                r0 = rBottom
                z0 = z
                costheta = Sqr(1# - Rnd)
                If (costheta > 0.99999) Then
costheta = 0.99999
                phi = 2 * Pi * Rnd
                sintheta = Sqr(1# - costheta ^ 2)
                vz = Cos(phi) * sintheta
                vy = Sin(phi) * sintheta
                vx = costheta
                rf = rBottom
                t = (vx * r0 + Sqr((vx ^ 2 + vy ^
2) * rf ^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)
                z = z0 + t * vz
            End If ' bottom cylinder re-emission

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```

If ((z >= lenBottom) And (z0 < lenBottom))
Then
    ' emitted below but going up
    ' find radius at lenBottom
    t = (lenBottom - z0) / vz
    r = Sqr((r0 - vx * t) ^ 2 + (vy *
t) ^ 2)
    If (r <= 1) Then
    ' continuing upward
    rf = 1#
    t = (vx * r0 + Sqr((vx ^ 2 + vy ^
2) * rf ^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)
    z = z0 + vz * t
    Else
    ' hit the upstream side of the accel
grid and is re-emitted downward
    r0 = r
    z0 = lenBottom
    costheta = Sqr(1# - Rnd)
    If (costheta > 0.99999) Then
costheta = 0.99999
    phi = 2 * Pi * Rnd
    sintheta = Sqr(1# - costheta ^ 2)
    vx = Cos(phi) * sintheta
    vy = Sin(phi) * sintheta
    vz = -costheta
    rf = rBottom
    t = (vx * r0 + Sqr((vx ^ 2 + vy ^
2) * rf ^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)
    z = z0 + vz * t
    End If
    End If ' end upward
    If ((z >= lenBottom) And (z <= Length))
Then
    ' hit the upper cylinder wall and is
re-emitted
    r0 = 1#
    z0 = z
    costheta = Sqr(1# - Rnd)
    If (costheta > 0.99999) Then
costheta = 0.99999
    phi = 2 * Pi * Rnd
    sintheta = Sqr(1# - costheta ^ 2)
    vz = Cos(phi) * sintheta
    vy = Sin(phi) * sintheta
    vx = costheta
    rf = 1#
    t = (vx * r0 + Sqr((vx ^ 2 + vy ^
2) * rf ^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)

```

```

        z = z0 + t * vz
        If (z < lenBottom) Then
            ' find z when particle hits the
bottom cylinder
                rf = rBottom
                If ((vx ^ 2 + vy ^ 2) * rf ^ 2
- (vy * r0) ^ 2 < 0#) Then
                    t = (vx * r0) / (vx ^ 2 +
vy ^ 2) 'if sqr arguement is less than 0 then set sqr term
to 0 12 May 2004
                Else
                    t = (vx * r0 + Sqr((vx ^ 2
+ vy ^ 2) * rf ^ 2 - (vy * r0) ^ 2)) / (vx ^ 2 + vy ^ 2)
                End If
                z = z0 + vz * t
            End If
        End If ' end upper cylinder emission
        If (z < 0#) Then
            notgone = False
        End If
        If (z > Length) Then
            iescape = iescape + 1
            vztot = vztot + vz
            notgone = False
        End If
        If (icount > 1000) Then
            notgone = False
            icount = 0
            nlost = nlost + 1
        End If
        Loop ' while
        If (maxcount < icount) Then maxcount = icount
    Next ipart ' particles
    Range("C11") = (rBottom ^ 2) * iescape / npart
    Range("C12") = maxcount
    Range("C13") = nlost
    vz0av = vz0tot / npart
    vzav = vztot / iescape
    DenCor = vz0av / vzav ' Downstream correction
factor
    End Sub ' Clausing

```